



**Question 1: [30 marks] [ILOs: a1,b7,c1,c7]**

a) The population of Mississippi during five census periods was as follows:

Year (x)	1891	1901	1911	1921	1931
Population (y) "in thousand"	46	66	81	93	101

Interpolate the population during 1925 by using Newton's interpolation.

b) Use Runge-Kutta method to obtain the approximate value  $y(0.1)$  where  $y(x)$  is a solution of second O.D.E.

$$y'' + 3xy' - 6y = 0, \text{ with initial condition } y(0) = 1, y'(0) = 0.1$$

c) Calculate  $\ln(2)$  by using Lagrange interpolation, where  $\ln(1)=0, \ln(4)=1.386294, \ln(6)=1.791759$

**Question 2: [30 marks] [ILOs: a1,b1,b7]**

a) Fit the curve  $y = ax^b e^{cx}$  to the following readings

x	1	2	3	4
y	3.6	5.2	6.8	8.8

b) By using Bisection method, find root of  $3x - e^{-x} = 0$  in the interval  $[0.25, 0.27]$  (correct to three decimal places).

c) By using eigenvalues and eigenvectors, find the solution of:

$$X' = \begin{bmatrix} 0 & 1 \\ -4 & 0 \end{bmatrix} X, \quad X(0) = \begin{bmatrix} 5 \\ 3 \end{bmatrix}$$

**Question 3: [30 marks] [ILOs: a1,b1]**

a) Use LU-Decomposition to find the inverse of  $A = \begin{pmatrix} 25 & 5 & 1 \\ 64 & 8 & 1 \\ 144 & 12 & 1 \end{pmatrix}$

b) Prove that  $\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$

**By using Gamma and Beta Functions, Find the following:**

c) The area between  $y = 4x^{3/2} e^{-x^{2/2}}, x = 0$

d) (i)  $\int_0^{\infty} \sqrt{y} e^{-y^3} dy$       (ii)  $\int_0^{\frac{\pi}{2}} \sin^6(\theta) d\theta$       (iii)  $\int_0^2 \frac{x^2}{\sqrt{2-x}} dx$

With my best wishes >>>>=====<<<< Dr. Manal Elsayed

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