

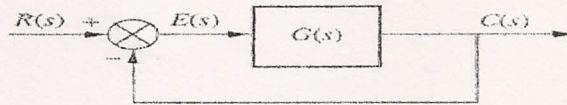


Intended Learning Outcomes (ILOs): [a1, a4, a12, b2, b6, b11, b12, b14, c3, c14]

Problem 1: (35 Marks) - (ILOs): [a1, a12, b2, b6, c3]

i. Construct the configuration of the electronic lag compensator using operational amplifiers and derive the transfer function of the compensator. (5 Marks)

ii. For a unity feedback system given below, with $G(s) = \frac{K}{s(s+5)(s+11)}$ (15 Marks)

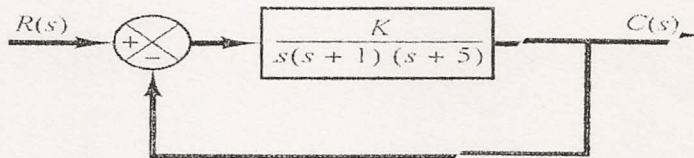


do the following

- Find the gain K , for the uncompensated system to operate with a 30% overshoot. (10 Marks)
- Find the peak time and K_v for the uncompensated system. (10 Marks)
- Design a lead compensator to decrease the peak time by a factor of 2, decrease the percent overshoot by a factor of 2, and improve the steady-state error by a factor of 30. Specify all poles, zeros and gains. (10 Marks)

Problem 2: (3 Marks) - - (ILOs): [a12, b2, b6, b11]

- Define gain margin, phase margin and explain graphically. What are the gain margin and the phase margin indicate? (10 Marks)
- Obtain the phase and gain margins of the system shown in following figure for the two cases where $K=10$ and $K=100$. (10 Marks)



c) Draw the polar plot of the system and Comment on the stability of the system. (10 Marks)

Problem 3 (30 Marks) - - (ILOs): [a1, b2, b14, c3, c14]

- What are controllability and observability of control systems? (5 Marks)
- For the following system, compute by hand the controllability matrix, observability matrix and determine whether the system is observable. (10 Marks)

$$\dot{x} = \begin{bmatrix} 1 & 1 & 2 \\ 3 & 5 & 8 \\ 13 & 21 & 34 \end{bmatrix} x + \begin{bmatrix} 1 \\ 1 \\ -1 \end{bmatrix} u$$

$$y = \begin{bmatrix} 0 & 3 & -5 \end{bmatrix} x$$

c) Find the transfer function and poles of the system represented in state space below. (10 Marks)

$$\dot{x} = \begin{bmatrix} 8 & -4 & 1 \\ -3 & 2 & 0 \\ 5 & 7 & -3 \end{bmatrix} x + \begin{bmatrix} -4 \\ -3 \\ 4 \end{bmatrix} u(t)$$

$$y = \begin{bmatrix} 2 & 8 & -2 \end{bmatrix} x \quad x(0) = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$