



جامعة كفرالشيخ - كلية الهندسة - قسم الهندسة الكهربائية

امتحان نهاية الفصل الاول للعام الجامعي 2017-2018

المتحن: د/علي صقر يوم الامتحان : 2018/1/14

الدرجة من 90 الفرقة 3 حاسبات المادة: تصميم الخوارزمات

5 M      الاجابة

Fullfill ilos :  $a_1, a_2, a_3, a_4,$

- 1- [15M] write an algorithm that search for n elements in a vector of m elements using linear search.

For (index= 1, index<=n, index++)

Key= item (index)

For (k= 1, k<=m, k++)

{if ( key= a[k]) break};

the expected number of comparisons. =  $n*m$

3 M

search for the number 48 .not exist

2 M

- 5 M write an insertion algorithms to sort the next numbers, then search for the number 54 after sorting, find number of comparisons.

|   |    |    |   |    |   |    |    |    |    |    |   |    |    |   |    |
|---|----|----|---|----|---|----|----|----|----|----|---|----|----|---|----|
| 6 | 11 | 12 | 4 | 15 | 7 | 19 | 22 | 23 | 25 | 29 | 3 | 41 | 54 | 5 | 64 |
|---|----|----|---|----|---|----|----|----|----|----|---|----|----|---|----|

Sorting using insertion algorithms.

|   |    |    |    |    |    |    |    |    |    |    |    |    |    |  |  |
|---|----|----|----|----|----|----|----|----|----|----|----|----|----|--|--|
| 6 |    |    |    |    |    |    |    |    |    |    |    |    |    |  |  |
| 6 | 11 |    |    |    |    |    |    |    |    |    |    |    |    |  |  |
| 6 | 11 | 12 |    |    |    |    |    |    |    |    |    |    |    |  |  |
| 4 | 6  | 11 | 12 |    |    |    |    |    |    |    |    |    |    |  |  |
| 4 | 6  | 11 | 12 | 15 |    |    |    |    |    |    |    |    |    |  |  |
| 4 | 6  | 7  | 11 | 12 | 15 |    |    |    |    |    |    |    |    |  |  |
| 4 | 6  | 7  | 11 | 12 | 15 | 19 |    |    |    |    |    |    |    |  |  |
| 4 | 6  | 7  | 11 | 12 | 15 | 19 | 22 |    |    |    |    |    |    |  |  |
| 4 | 6  | 7  | 11 | 12 | 15 | 19 | 22 | 23 |    |    |    |    |    |  |  |
| 4 | 6  | 7  | 11 | 12 | 15 | 19 | 22 | 23 | 25 |    |    |    |    |  |  |
| 4 | 6  | 7  | 11 | 12 | 15 | 19 | 22 | 23 | 25 | 29 |    |    |    |  |  |
| 3 | 4  | 6  | 7  | 11 | 12 | 15 | 19 | 22 | 23 | 25 | 29 |    |    |  |  |
| 3 | 4  | 6  | 7  | 11 | 12 | 15 | 19 | 22 | 23 | 25 | 29 | 41 |    |  |  |
| 3 | 4  | 6  | 7  | 11 | 12 | 15 | 19 | 22 | 23 | 25 | 29 | 41 | 54 |  |  |

|   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|
| 3 | 4 | 5 | 6 | 7 | 11 | 12 | 15 | 19 | 22 | 23 | 25 | 29 | 41 | 54 |    |
| 3 | 4 | 5 | 6 | 7 | 11 | 12 | 15 | 19 | 22 | 23 | 25 | 29 | 41 | 54 | 64 |

54 exists at location n-1, number of comparisons  $O(n)$

fulfill

2- [5M] To compute value of a polynomial, 2 algorithms may be used:

$$\text{Algorithm 1: } p(x) = \sum a^i x^i = a_0 + a_1 x^1 + a_2 x^2 + a_3 x^3 + \dots + a_{n-1} x^{n-1} + a_n x^n$$

C<sub>2</sub>, C<sub>4</sub>

$$\text{Algorithm 2: } p(x) = ((\dots(a_n x + a_{n-1})x + a_{n-2})x + \dots)x + a_1)x + a_0$$

Which algorithm is better, who many operations in each algorithm.

**Algorithm 2 is faster, number of multiplications  $O(n)$ , while algorithm 1 necessitates number of multiplications  $O(n^2)$**

3- [15M] Write an algorithm that sorts n elements using merge sort algorithm.  
Apply for the next data, define number of comparisons,

2, 22, 41, 64, 14, 5, 29, 55, 17, 7, 25, 33, 11, 43, 50, 46, 82, 19, 23, 54

2, 22, 41, 64, 5, 14, 29, 55, 7, 17, 25, 33, 11, 43, 46, 50, 19, 82, , 23, 54

2, 22, 41, 64, 5, 14, 29, 55, 7, 17, 25, 33, 11, 43, 46, 50, 19, 23, 54, 82

2, 5, 14, 22, 29, 41, 55, 64, 7, 11, 17, 25, 33, 43, 46, 50, 19, 23, 54, 82

2, 5, 7, 11, 14, 17, 22, 25, 29, 33, 41, 43, 46, 50, 55, 64, 19, 23, 54, 82

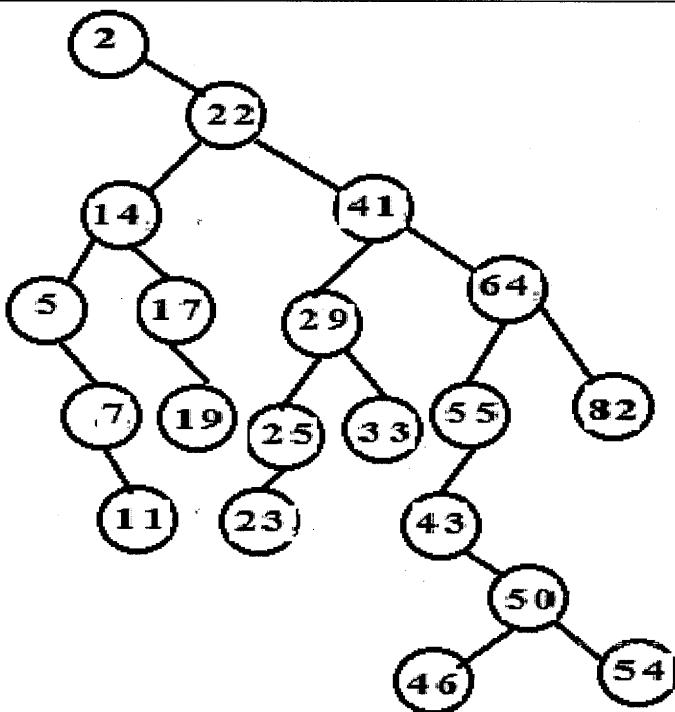
2, 5, 7, 11, 14, 17, 19, 22, 23, 25, 29, 33, 41, 43, 46, 50, 54, 55, 64, 82

Number of operations  $O(n \log n)$

construct a binary tree for sorting, compare complexity of the two algorithms.

Number of operations  $O(n \log n)$

fulfill C<sub>2</sub>, C<sub>4</sub>



Using infix scan:

2, 5, 7, 11, 14, 17, 19, 22, 23, 25, 29, 33, 41, 43, 46, 50, 54, 55, 64, 82

4-[5M] Let string : R= abcdefg56789, reverser= 98765gfedcba,

S= ABCDEFGHIJKLMNOPQRSTUVWXYZ1234567890,

Write functions to compute: length of S, substring(S, 10,5), index (S, MNO), concatenate (S,R), delete(S, 5,5), insert (S,12,R), replace(S, PQR, reverser),

len (S)= 36

substring(S, 10,5)= JKLMN,

index (S, MNO)= 12,

concatenate (S,R)= ABCDEFGHIJKLMNOPQRSTUVWXYZ1234567890 abcdefg56789,

delete(S, 5,5)= ABCDJJKLMNOPQRSTUWVXYZ1234567890,

insert (S,12,R)= ABCDEFGHIJKL abcdefg56789MNOPQRSTUWVXYZ1234567890,

replace(S, PQR, reverser)= ABCDEFGHIJKLMNO98765gfedcba STUVWXYZ1234567890,

5-[10M] Use stack to generate postfix expressions for the next infix expressions:

(a\*b) ^c - (c-d)\*E / (x^y). Use the binary tree to generate the postfix expression.

|   |   |
|---|---|
| b | ) |
| a | * |
|   | ( |

|       |   |
|-------|---|
| c     |   |
| (a*b) | ^ |

(5M)  
self || ds

|                  |   |
|------------------|---|
|                  | ) |
| d                | - |
| c                | ( |
| $(a*b) \wedge c$ | - |

|                  |          |
|------------------|----------|
|                  | )        |
| y                | $\wedge$ |
| x                | (        |
| E                | /        |
| $(c-d)$          | *        |
| $(a*b) \wedge c$ | -        |

|                  |   |
|------------------|---|
| $(x \wedge y)$   |   |
| E                | / |
| $(c-d)$          | * |
| $(a*b) \wedge c$ | - |

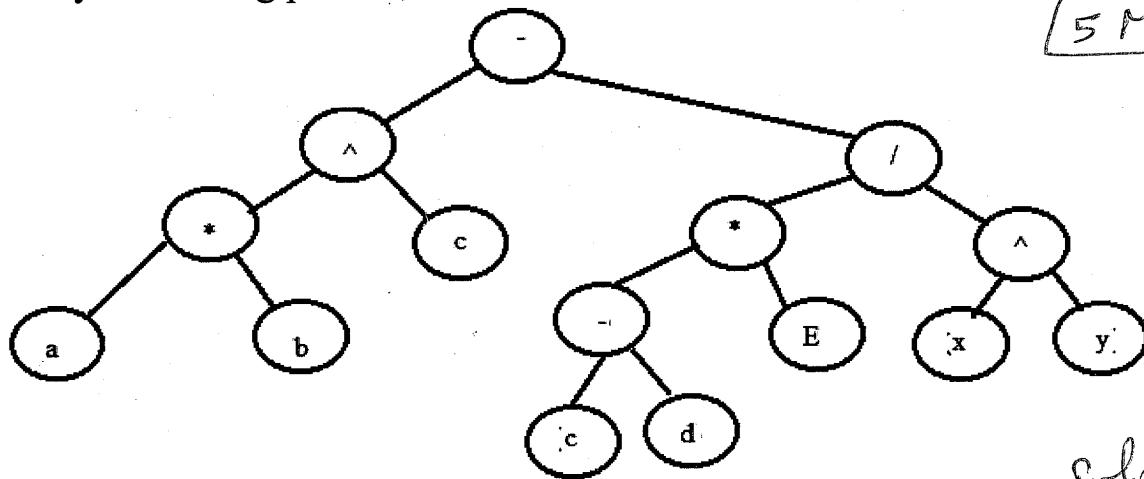
|                    |   |
|--------------------|---|
| E / (x $\wedge$ y) |   |
| $(c-d)$            | * |
| $(a*b) \wedge c$   | - |

|                            |   |
|----------------------------|---|
| $(c-d) * E / (x \wedge y)$ |   |
| $(a*b) \wedge c$           | - |

$(a*b) \wedge c - (c-d) * E / (x \wedge y)$

Binary tree: using postfix, reads: a b \* c  $\wedge$  c d - E \* x y  $\wedge$  / -

5 M



self C<sub>2</sub>

6-[15M] Write an algorithm that sorts a vector of n elements, using radix sort technique. Apply for the next data, deduce number of comparisons in each case. Delete the items 15, 54. Find the new linked list. Write the algorithm for deletion.

12, 2, 41, 64, 14, 15, 29, 55, 17, 6, 25, 33, 61, 43, 50, 46, 82, 19, 23, 56

1<sup>st</sup> (right) digit sorting:

| <b>0</b> | <b>1</b> | <b>2</b> | <b>3</b> | <b>4</b> | <b>5</b> | <b>6</b> | <b>7</b> | <b>8</b> | <b>9</b> |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 50       | 41       | 12       | 33       | 64       | 15       | 6        | 17       |          | 29       |
|          | 61       | 2        | 43       | 14       | 55       | 46       |          |          | 19       |
|          |          | 82       | 23       |          | 25       | 56       |          |          |          |

The pseudo ordered set is

**50,41,61, 12,2,82, 33,43,23,64,14,15,55,25,6,46,56,17,29,19**

The 2<sup>nd</sup> digit sorting:

| <b>0</b> | <b>1</b> | <b>2</b> | <b>3</b> | <b>4</b> | <b>5</b> | <b>6</b> | <b>7</b> | <b>8</b> | <b>9</b> |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 2        | 12       | 23       | 33       | 41       | 50       | 61       |          | 82       |          |
| 6        | 14       | 25       |          | 43       | 55       | 64       |          |          |          |
|          | 15       | 29       |          | 46       | 56       |          |          |          |          |
|          | 17       |          |          |          |          |          |          |          |          |
|          | 19       |          |          |          |          |          |          |          |          |

The ordered set is :

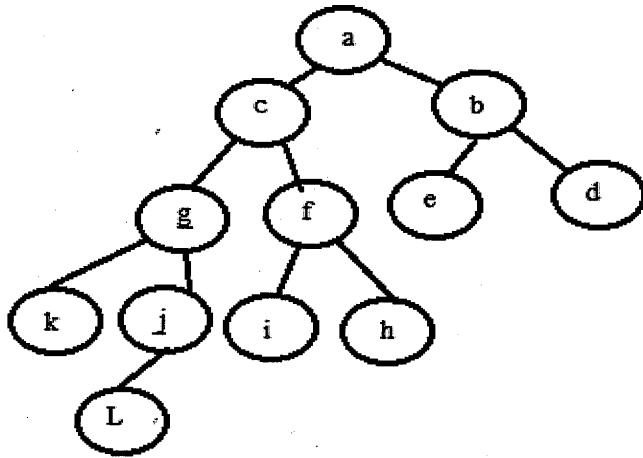
**2,6,12,14,15,17,19,23,25,29,33,41,43,46,50,55,56,61,64,82**

Use linked list to sort these items:

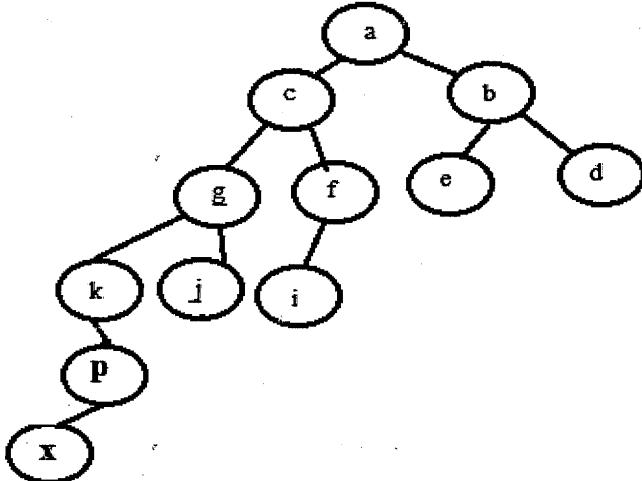
|           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| <b>1</b>  | <b>2</b>  | <b>3</b>  | <b>4</b>  | <b>5</b>  | <b>6</b>  | <b>7</b>  | <b>8</b>  | <b>9</b>  | <b>10</b> | <b>11</b> | <b>12</b> | <b>13</b> | <b>14</b> | <b>15</b> | <b>16</b> | <b>17</b> | <b>18</b> | <b>19</b> | <b>20</b> |
| <b>12</b> | <b>2</b>  | <b>41</b> | <b>64</b> | <b>14</b> | <b>15</b> | <b>29</b> | <b>55</b> | <b>17</b> | <b>6</b>  | <b>25</b> | <b>33</b> | <b>61</b> | <b>43</b> | <b>50</b> | <b>46</b> | <b>82</b> | <b>19</b> | <b>23</b> | <b>56</b> |
| <b>5</b>  | <b>S</b>  | <b>14</b> | <b>17</b> | <b>6</b>  | <b>9</b>  | <b>12</b> | <b>20</b> | <b>18</b> | <b>1</b>  | <b>7</b>  | <b>3</b>  | <b>4</b>  | <b>16</b> | <b>8</b>  | <b>15</b> | <b>0</b>  | <b>19</b> | <b>11</b> | <b>13</b> |
|           | <b>10</b> |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |           |

7-[10M] construct the next tree, regarding the next double linked list. Write the corresponding algorithm. Traverse the tree using postfix notation.

|       | <b>1</b> | <b>2</b> | <b>3</b> | <b>4</b> | <b>5</b> | <b>6</b> | <b>7</b> | <b>8</b> | <b>9</b> | <b>10</b> | <b>11</b> | <b>12</b> |
|-------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|-----------|-----------|
| Right | 2        | 4        | 6        | 0        | 0        | 8        | 10       | 0        | 0        | 0         | 0         | 0         |
| info  | a        | b        | c        | d        | e        | f        | g        | h        | i        | j         | k         | L         |
| left  | 3        | 5        | 7        | 0        | 0        | 9        | 11       | 0        | 0        | 12        | 0         | 0         |



Delete elements h, L. insert item P to be a right child for item k. P has a left child x, and no right one.



|       | 1 | 2 | 3 | 4 | 5 | 6 | 7  | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|-------|---|---|---|---|---|---|----|---|---|----|----|----|----|----|
| Right | 2 | 4 | 6 | 0 | 0 | 0 | 10 | 0 | 0 | 0  | 13 | 0  | 0  | 0  |
| info  | a | b | c | d | e | f | g  | h | i | j  | k  | L  | p  | x  |
| left  | 3 | 5 | 7 | 0 | 0 | 9 | 11 | 0 | 0 | 0  | 0  | 0  | 14 | 0  |

8-[10M] Let a set of tasks to be processed in a FCFS\_queue using one server, find the average completion time, average service time, average waiting time, consider front =1, rear= 13 . find number of waiters in queue (queue length).

by C<sub>2</sub>

| Task num.               | 1  | 2  | 3  | 4  | 5  | 6   | 7   | 8   | 9   | 10  | 11  | 12  | 13  |
|-------------------------|----|----|----|----|----|-----|-----|-----|-----|-----|-----|-----|-----|
| Expected execution time | 25 | 22 | 12 | 20 | 2  | 50  | 30  | 10  | 2   | 20  | 40  | 10  | 5   |
| waiting                 | 0  | 25 | 47 | 59 | 79 | 81  | 131 | 161 | 171 | 173 | 193 | 233 | 243 |
| completion time         | 25 | 47 | 59 | 79 | 81 | 131 | 161 | 171 | 173 | 193 | 233 | 243 | 248 |
| Number of waiters       | 12 | 11 | 10 | 9  | 8  | 7   | 6   | 5   | 4   | 3   | 2   | 1   | 0   |